

**Speaker:** Carsten Peterson

**Title:** Quantum ergodicity on Bruhat-Tits buildings of type  $\tilde{A}_2$

**Abstract:** Quantum ergodicity refers to equidistribution results for eigenfunctions of Laplacian-like operators which arise from "quantizing" an ergodic dynamical system. Recently, Anantharaman and Le Masson showed such a result for regular graphs (some of which arise as quotients of buildings for  $SL(2, K)$  where  $K$  is a non-Archimedean local field) and Brumley and Matz, building on work of Le Masson and Sahlsten, showed such a result for locally symmetric spaces associated to  $SL(n, \mathbb{R})$ . We establish analogous results for  $SL(3, K)$ . Specifically, consider a sequence  $\{X_n\}$  of compact quotients of the Bruhat-Tits building associated to  $SL(3, K)$  which converge in the sense of Benjamini-Schramm to the building. We prove that on average joint eigenfunctions of the spherical Hecke algebra of  $PGL(3, K)$  acting on  $L^2(X_n)$  (thought of as functions on the vertices) converge in a weak-\* sense to the counting measure on vertices as  $n \rightarrow \infty$ . Some ingredients of the proof are the explicit decomposition of  $L^2(PGL(3, K)/PGL(3, \mathcal{O}_K))$  into irreducibles as a representation of  $PGL(3, K)$ , a mean ergodic theorem for convolution operators on semisimple Lie groups, geometry of affine buildings, and Brion's formula for exponential sums over polytopes.