List of Topics

1. Measure theoretic preliminaries

Sections: 2.1-2.3 and 2.5.

Content: Basic notation. Borel and Hausdorff measures. Minkowski and Packing dimensions. Energy integrals and Frostman's lemma. *Daphné Baudeau: Nov 2*

2. Fourier transforms

Sections: 3.4-3.8

Content: The Fourier transform of Riesz kernels. Energy integrals of measures. Salem sets and Fourier dimension. Spherical and ball averages. *Niklas Herrigel: Nov 9*

 Hausdorff dimension of projections and distance sets Sections: 4.1-4.3.
Content: Projections. Distance sets. Dimension of Borel rings.

William William: Nov 16

4. Exceptional projections and Sobolev dimension Sections: 5.1-5.3.

Content: Exceptional sets for one-dimensional projections. Sobolev dimension. Higher dimensional projections. *Christoph Heidgress: Nov 23*

5. Slices of measures and intersections with planes
Sections: 6.1-6.3.
Content: Sliced measures and estimates for enrgy integrals. Dimensions

of plane sections. Measures on graphs. Leo Diedering: Nov 30

6. Intersections of general sets and measures

Sections: 7.1-7.2.

Content: Intersection measures and energy estimates. Dimensions of intersections of sets.

7. Cantor measures

Sections: 8.1-8.3. Content: Symmetric Cantor sets and measures. Pisot numbers and the corresponding measures. Self-similar measures.

- Projections of the four-corner Cantor set Sections: 10.1-10.4.
 Content: Peres–Simon–Solomyak proof. Kenyon's tilings and projections. Average length of projections.
- Besicovitch sets Sections: 11.1-11.5 Content: Existence and Hausdorff dimension of Besicovitch sets. Nikodym sets. Lines vs. line segments. Furstenberg sets.

10. Bernoulli convolutions and Brownian motion Sections: 9.1 and 12.1-12.2.

Content: Absolute continuity of the Bernoulli convolutions. Facts on Brownian motion. Dimension of Brownian trajectories.