The Consistency Strength of the Negation of the Singular Cardinal Hypothesis Without the Axiom of Choice

by Peter Koepke

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Abstract

We show - joint with Arthur Apter - that the consistency strengths of the theories $ZF + \neg$ SCH and ZFC + "there exists a measurable cardinal" are equal, where \neg SCH is interpreted as: there is a singular cardinal κ such that $\forall \nu \in [\omega, \kappa) \mathcal{P}(\nu) \sim \nu^+$ and there exists a *surjection* from $\mathcal{P}_{\leqslant \operatorname{cof}(\kappa)}(\kappa)$ onto κ^{++} . The proofs involve a standard application of the DODD-JENSEN core model theory and choiceless submodels of generic extensions by parallel PRIKRY forcing for a sequence of κ^{++} distinct normal measures on κ .