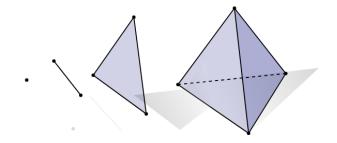
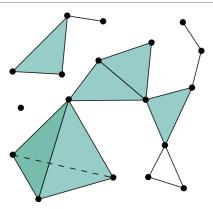
What are...simplicial complexes?

Or: Triangles everywhere

Lots of triangles



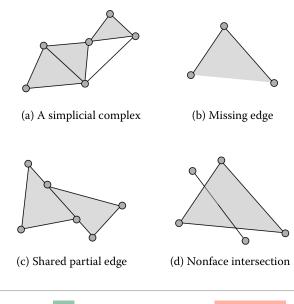
- ► A 0 dimensional triangle is a point
- ► A 1 dimensional triangle is a line
- ► A 2 dimensional triangle is a solid triangle
- ► A 3 dimensional triangle is a solid tetrahedron
- ► An *n* dimensional triangle is called an *n* simplex



▶ The boundary of an *n* simplex is made of n-1 simplex

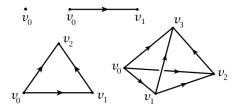
• Gluing simplices along their boundary gives simplicial complexes

Not everything is allowed



(a) is ok but (b), (c) and (d) are not allowed

An *n* simplex for $v_0, ..., v_n$ is smallest convex set in \mathbb{R}^{n+1} containing $v_0, ..., v_n$ that do not lie in a hyperplane of dimension less than *n*



If we delete one of the n + 1 vertices of an n simplex, then the remaining n vertices span an (n - 1) simplex, called a face 3d terminology Sometimes one needs an orientation, but this is ignored in this video

A simplicial complex Δ is a set of simplices satisfying

- Every face of a simplex from Δ is also in Δ (b) from before
- ► A $\neq \emptyset$ intersection of 2 simplices in Δ is a face of both (c),(d) from before

Abstract simplicial complexes Δ_{ab} are collections of non-empty sets satisfying $(X \in \Delta_{ab} \text{ and } Y \subset X) \Rightarrow (Y \in \Delta_{ab})$ These can be geometrically realized into simplicial complexes **Example** The abstract standard 2-simplex and its geometric realization: $\Delta_{ab}^{2} = \left\{ \begin{bmatrix} v_{0} \end{bmatrix}, \begin{bmatrix} v_{1} \end{bmatrix}, \begin{bmatrix} v_{2} \end{bmatrix}, \begin{bmatrix} v_{0}, v_{1} \end{bmatrix}, \begin{bmatrix} v_{0}, v_{1} \end{bmatrix}, \begin{bmatrix} v_{0}, v_{1}, v_{2} \end{bmatrix}, \begin{bmatrix} v_{0},$ $\left[V_{2} \right]$ $[V_0, V_1]$ $[v_1, v_2]$ $[V_0, V_1, V_2]$

Thank you for your attention!

I hope that was of some help.